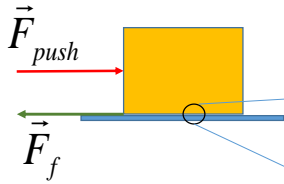


Friction



No movement: $F_{net} = 0$ $F_{push} = F_f$

The force of the push can rise: as long as there is no movement: the frictional force rises the same amount.

$$F_f = \mu_s \cdot F_n \quad F_f \leq \mu_s \cdot F_n$$

Static coefficient of friction

Movement:

$$F_f = \mu_k \cdot F_n$$

Kinetic coefficient of friction

Object accelerates: $F_{push} > F_f$

Object has constant speed: $F_{push} = F_f$

Friction

Experimental measurement of coefficient of friction

No movement:

$$\Sigma F_x = mg \cdot \sin \alpha - F_f$$

$$\Sigma F_y = F_n - mg \cdot \cos \alpha$$

$$mg \cdot \sin \alpha = F_f$$

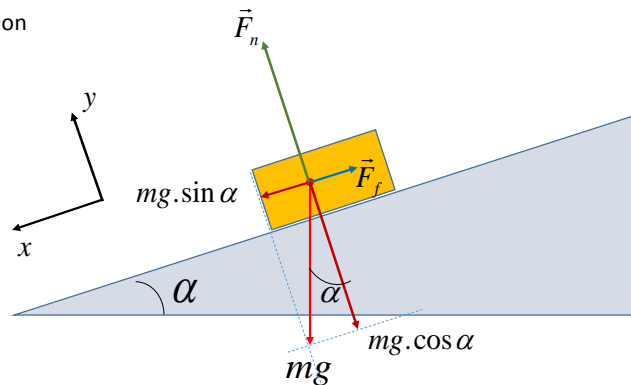
$$F_n = mg \cdot \cos \alpha$$

$$mg \cdot \sin \alpha = \mu \cdot F_n$$

~~$$mg \cdot \sin \alpha = \mu \cdot mg \cdot \cos \alpha$$~~

$$\frac{\sin \alpha}{\cos \alpha} = \mu$$

$$\tan \alpha = \mu$$



Friction

Example: An object with a 30,0 kg mass is on a surface inclined to the horizontal with an angle of 20,0°. The block would start sliding down, but when exerting a downward pushing force of 100 N as indicated on the drawing, The block is at the point of not sliding. Calculate the coefficient of friction.

$$\Sigma F_y = 0 = F_n - mg \cdot \cos \alpha - F_{push}$$

$$F_n = mg \cdot \cos \alpha + F_{push}$$

$$F_n = 30,0 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} \cdot \cos 20,0 + 100 = 377 \text{ N}$$

$$\Sigma F_x = 0 = mg \cdot \sin \alpha - F_f$$

$$mg \cdot \sin \alpha = F_f$$

$$F_f = 30,0 \text{ kg} \cdot 9,81 \frac{\text{N}}{\text{kg}} \cdot \sin 20,0 = 101 \text{ N}$$

$$F_f = \mu \cdot F_n \quad \mu = \frac{F_f}{F_n}$$

$$\mu = \frac{101 \text{ N}}{377 \text{ N}} = 0,268$$

